

Diagnostic methodology of cardiac dynamics based on the Zipf-Mandelbrot law: evaluation with 50 patients

Metodología diagnóstica de la dinámica cardíaca basada en ley de Zipf-Mandelbrot: evaluación con 50 pacientes

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ABSTRACT

Objective: Zipf-Mandelbrot law has been used to assess the complexity of cardiac systems. The objective of this work is to corroborate the clinical applicability of a diagnostic methodology developed from Zipf-Mandelbrot law, in the differentiation of normality and acute cardiac disease. **Material and methods:** there were taken 50 continuous electrocardiographic Holter monitoring records, 20 normal and 30 with acute alterations of the cardiac dynamics. The frequencies of occurrence of heart rates in ranges of 15 lat/min were organized hierarchically to demonstrate the hyperbolic behavior of dynamics and to apply the Zipf-Mandelbrot law. A linearization was performed and the statistical fractal dimension of each dynamic was obtained, giving rise to the mathematical diagnosis. Sensitivity, specificity and Kappa coefficient were calculated. **Results:** The values of the statistical fractal dimension of the acute cardiac dynamics were between 0.7123 and 0.9327, whereas for the normal dynamics were found between 0.4253 and 0.6698, evidencing quantitative differences between states of normality and disease. Sensitivity and specificity values of 100% were found and the kappa coefficient was 1. **Conclusions:** The clinical and diagnostic utility of the mathematical methodology based on Zipf-Mandelbrot law was verified, observing a decrease of dynamics complexity in cases of acute heart disease.

RESUMEN

Objetivo: La ley de Zipf-Mandelbrot ha sido utilizada con el fin de evaluar la complejidad de los sistemas cardíacos. El objetivo de este trabajo es corroborar la aplicabilidad clínica de una metodología diagnóstica desarrollada a partir de la ley de Zipf-Mandelbrot, en la diferenciación de normalidad y enfermedad cardíaca aguda. **Material y métodos:** Se tomaron 50 Holter cardíacos (monitoreo electrocardiográfico continuo ambulatorio), 20 normales y 30 con alteraciones agudas de la dinámica cardíaca. Se organizaron jerárquicamente las frecuencias de aparición de frecuencias cardíacas en rangos de a 15 lat/min, para evidenciar el comportamiento hiperbólico de las dinámicas y aplicar la ley de Zipf-Mandelbrot. Se realizó una linealización y se obtuvo la dimensión fractal estadística de cada dinámica, dando lugar al diagnóstico matemático. Fueron calculadas la sensibilidad, especificidad y el coeficiente Kappa. **Resultados:** Los valores de la dimensión fractal estadística de las dinámicas cardíacas agudas se encontraron entre 0.7123 y 0.9327, mientras que para las dinámicas normales se hallaron entre 0.4253 y 0.6698, evidenciando diferencias cuantitativas entre estados de normalidad y enfermedad. Se encontraron valores de sensibilidad y especificidad del 100% y el coeficiente kappa fue de 1. **Conclusiones:** Fue comprobada la utilidad clínica y diagnóstica de la metodología matemática basada en la ley de Zipf-Mandelbrot, observando un decremento de la complejidad de la dinámica en casos de enfermedad cardíaca aguda.

INTRODUCTION

Euclidean geometry allows the quantification of regular objects; however, it presents

limitations in the measurement of irregular objects.¹ In that order of ideas, Mandelbrot proposed a geometry capable of characterizing irregular objects based on the fractal dimension.

Statistical fractals are understood as systems that can be characterized by the distribution of frequencies appearance of certain variables, organized in a hierarchical way. In the mentioned systems, the statistical fractal dimension is measured, calculated by the Zipf-Mandelbrot law. Zipf assigned ranges to frequencies of occurrence of words in a text, evidencing a hyperbolic behavior of the phenomenon.² Then, Mandelbrot performed a logarithmic linearization of the previously mentioned behavior and calculated the statistical fractal dimension, variable that measures the degree of complexity of a system, as the inverse of the slope of the graph.³

With the statistical fractal dimension it was possible to determine the loss of complexity in the texts of nuns studying with Alzheimer's.⁴

Cardiovascular diseases are the leading cause of mortality worldwide. Only in 2012 around 17.5 million people died from these diseases,⁵ reason why they have a great preponderance in the different health systems. In cardiology, parameters have been sought to establish differences between normality and disease. As part of that search, the analysis of heart rate variability has been used with some frequency,⁶ whose alterations have been linked to some cardiovascular diseases.^{7,8} From new perspectives, studies have shown the non-linear behavior of the cardiac system, which can even have chaotic patterns,^{9,10} whose measurement is possible through fractal geometry, used to evaluate different structures of the human body.^{11,12}

The variability of the heart rate has been analyzed from non-linearity;¹³ with the called multifractal analysis, it has been possible to evaluate the autonomic regulation of heart rhythm in the context of ischemic episodes.¹⁴ Additionally, spectral analyzes have been used and an attempt has been made to establish their relationship with patient mortality, especially after suffering acute myocardial infarction;¹⁵ Likewise, the complexity of the dynamics has been associated with the variability of the heart rate¹⁶ and two different types of non-linear dynamics have been evidenced in short registration periods.¹⁷ However, investigations have shown the imperative need to perform more accurate analysis.

Perspectives based on modern theoretical physics and the theory of dynamic systems, have allowed the advent of new research in fetal cardiac systems,^{18,19} of adults^{20,21} and neonatal,²² obtaining objective and reproducible diagnoses. Also, diagnoses have been made in patients with arrhythmias.^{23,24} An exponential law of chaotic cardiac dynamics was also developed²⁵ and a mathematical method based on the proportions of entropy allowed the establishment of differentiations between normality and pathological states.^{26,27}

It has also allowed established mathematical parameters indicative of evolution towards acute disease, independent of population or statistical analysis. A diagnostic methodology based on the Zipf-Mandelbrot law, allowed to demonstrate the degree of complexity of the normal cardiac systems and in states of exacerbation, this complexity being greater in the case of normal systems, an aspect that can be evidenced by the statistical fractal dimension.²⁸

The objective of this work is to confirm the clinical applicability of a methodology based on the Zipf-Mandelbrot law in the context of a blind study with 50 electrocardiographic tracings of normal and pathological cases.

MATERIAL Y METHODS

Definitions:

Statistical fractal dimension: to establish the statistical fractal dimension of Zipf-Mandelbrot, a logarithmic linearization is performed by applying the least squares method, finding the negative multiplicative inverse of the slope, corresponding to the statistical fractal dimension:

$$D = \frac{\text{Log}_{10}(\sigma + V)}{\text{Log}_{10}(F/P)} \quad \text{Equation \#1}$$

being, D: the fractal dimension; σ : the range for each frequency, P: the frequency of appearance of the heart rate. V: is defined by $V = 1/(N-1)$ in which N: is the number of frequencies measured; F: is a secondary cofactor in linearization, obtained from the application of the least squares method.

Procedure

50 ambulatory and continuous electrocardiographic recordings were taken, for at least 21 hours of subjects over 21 years of age, of Insight group databases. These records were for 20 patients with clinical evaluation within normal limits and 30 patients with acute cardiac pathologies, according to the criteria of an expert electrophysiologist, based on conventional medical protocols. Initially, the clinical findings were masked.

From each record, the values of maximum and minimum heart rate were taken in each hour. Then, a count was made of the number of heart rates found in each range of 15 beats/min. The frequency of appearance of the ranges of 15 beats/min was calculated. Subsequently, the Zipf-Mandelbrot law was applied to these values; for this, the frequencies of appearance of the ranges were ordered from highest to lowest, an integer was assigned to each of them, starting with one and increasing by one unit for the following frequencies of appearance, that were ordered in a hierarchical way. The data was graphed to corroborate the hyperbolic behavior and later give rise to the application of the law (see equation #1). A logarithmic linearization using the least squares method was applied to the scatter of points obtained in the graph, and the correlation coefficient (r^2) of the line of greatest adjustment of this point dispersion was established. Finally, the statistical fractal dimension of each dynamic was found and, consequently, its degree of complexity.

For the purposes of the statistical analysis, the clinical diagnoses were unmasked. A comparison was made between the mathematical methodology and the conventional diagnosis, taken as gold standard, for which specificity and sensitivity were calculated using a binary classification, where the true positives correspond to the number of patients with diagnosis of abnormality according to the gold standard and the mathematical method, false positives correspond to cases with mathematical values suggestive of abnormality and with a clinical diagnosis of normality, false negatives are cases with mathematical values indicative of

normality and clinical diagnosis of abnormality, the true negatives correspond to the records diagnosed both clinically and mathematically as normal.

The agreement between the mathematical diagnosis and the conventional clinician was evaluated, using the kappa coefficient, through the following formula:

$$K = \frac{Co - Ca}{To - Ca} \text{ Equation \#2}$$

Co corresponds to the number of matches observed, that is, the number of patients diagnosed equally by the mathematical method and the conventional diagnosis. To corresponds to the total number of cases. Ca represents the matches attributed to chance, calculated by the formula:

$$Ca = [(f_1 \times C_1)/To] + [(f_2 \times C_2)/To] \text{ Equation \#3}$$

f_1 corresponds to the number of patients with mathematical values indicative of normality, C_1 corresponds to the number of patients with a clinical diagnosis of normality, f_2 corresponds to the number of patients with mathematical values indicative of abnormality, C_2 represent cases conventionally diagnosed as abnormal and To represents the total of cases.

Ethical aspects

This study is governed by the ethical principles contemplated in the Declaration of Helsinki of the World Medical Association and adopts Resolution 8430 of 1993 of the Ministry of Health of Colombia. It is declared as a minimum risk investigation, given that mathematical calculations are made based on non-invasive examinations and paraclinics previously prescribed according to conventional medical protocols, protecting the information and integrity of the participants.

RESULTS

In the analysis of the degree of complexity of the dynamics, it was evidenced that the statistical fractal dimensions of the normal cases had values between 0.7123 and 0.9327 and the values for the correlation coefficient of the highest-fit lines

(r^2) were found between 0.7714 and 0.9742; (Figure 1) whereas for the cases of patients studying with acute pathologies the fractal dimensions were between 0.4253 and 0.6698 and the correlation factor was between 0.6658 and 0.9513 (Table I and Figure 2).

In the diagnostic test to confirm the applicability and clinical reproducibility of the methodology with respect to conventional clinical evaluation, had sensitivity and specificity values of 100%, and the Kappa coefficient was 1, which corroborated the ability of the methodology to

differentiate with mathematical values the normal cardiac dynamics from acute pathologies.

DISCUSSION

This is the first work in which the clinical applicability and diagnostic capacity of a methodology based on the Zipf-Mandelbrot law is corroborated, through a blind study with 50 normal cardiac and pathological dynamics, from which the degree of complexity of cardiac systems was determined by the statistical fractal dimension, obtaining objective and reproducible results, and reaching the maximum values of sensitivity and specificity. With the analysis of the hierarchical order of the cardiac frequencies it was possible to observe a hyperbolic behavior of the same, evidencing the self-organization of the cardiac system and indicating that the complexity of said system is inversely proportional to the degree of aggravation of the dynamics.

Previously, the greater degree of complexity of the normal versus the pathological dynamics was evidenced and the mathematical values that are associated with exacerbation were established,²⁸ which was confirmed in the present investigation.

From the perspective within which the presented method is framed, other investigations have been developed, giving rise to methodologies capable of differentiating normality, evolution and acute disease; such is the case of proportional entropy, a method that allows to establish high precision diagnoses.²⁷ Also, an exponential mathematical law was developed that allowed the establishment of the totality of chaotic cardiac attractors and the realization of differentiations between normality, disease and evolutive states^{23,25} with greater precision compared to the methods developed for this purpose.^{16,17} Rodríguez and cols.^{29,30} used the theory of probability in order to develop a diagnostic methodology, whose clinical applicability was confirmed. The methodology based on the Zipf-Mandelbrot law, allows the evaluation of the degree of complexity of cardiac systems with clear numerical parameters, independent of causal variables. Its simplicity is highlighted, because by means of a single

Table I. Statistical fractal dimension (DF) and correlation coefficient (r^2).

No.	Normal		Acute Myocardial Infarction	
	DF	r^2	DF	r^2
1	0.8195	0.8422	0.5337	0.9139
2	0.8253	0.9096	0.6474	0.8794
3	0.7692	0.8260	0.5895	0.6730
4	0.9309	0.9696	0.6674	0.6688
5	0.7922	0.8402	0.5036	0.8781
6	0.7637	0.8982	0.4738	0.8833
7	0.8665	0.9038	0.4323	0.7852
8	0.9109	0.8929	0.6191	0.9398
9	0.8291	0.8375	0.6234	0.8822
10	0.7289	0.8172	0.4255	0.8852

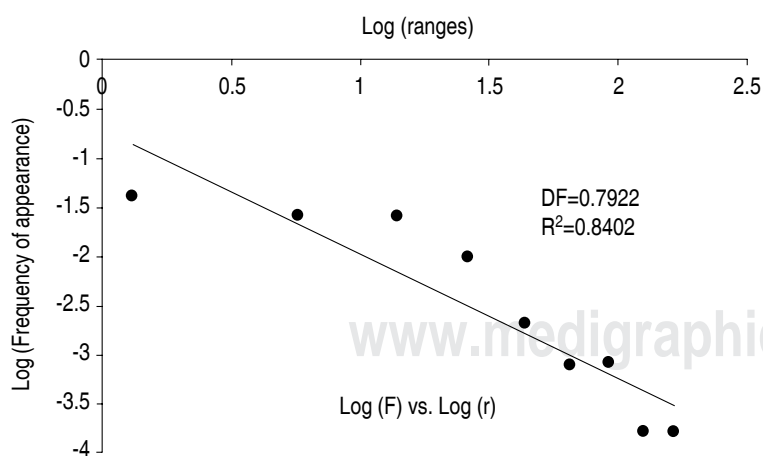


Figure 1. Logarithmic linearization corresponding to case 5 of table I with normal dynamics. Note the difference with figure 2, this presents a higher degree of complexity than that of figure 1.

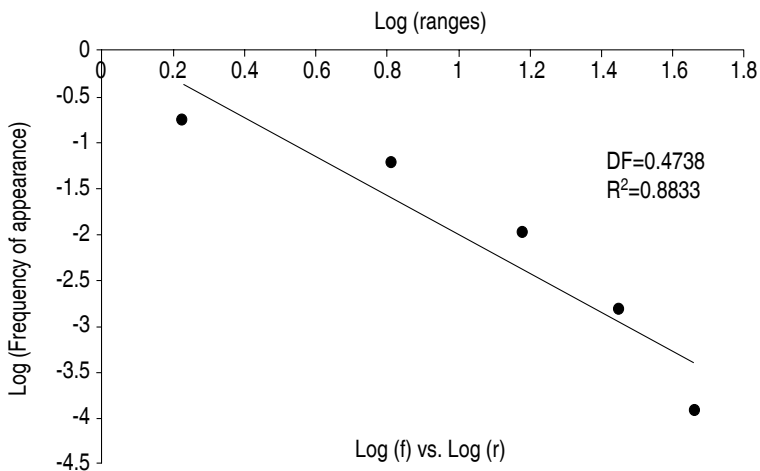


Figure 2. The logarithmic linearization of the frequency distribution in heart rate ranges of case 6 of *table I* with acute pathology can be observed. Here on the X axis is the logarithm of the range assigned by the application of Zipf's law, and on the Y axis is the logarithm of the frequency of appearance of each range. These ranges are ranges of 15 beats/min of heart rates.

parameter the degree of complexity of cardiac dynamics is established and subsequently the mathematical diagnosis.

Goldberger et al.¹⁰ in the context of dynamic systems allowed the development of a new conception of normality and disease, according to which, the abnormality is associated with very regular or extremely random states, while normality is in the intermediate between these states. Huikuri and cols.,³¹ performed a characterization of cardiac behavior in patients with acute myocardial infarction and a decreased ejection fraction, establishing predictive mortality rates. However, more studies are required to confirm the applicability of this and other methods based on dynamic systems.³² The presented methodology follows this line of thought and also allows the quantification of cardiac dynamics based on the statistical fractal dimension, which differentiates between disease and normality. In the research carried out, the mathematical order underlying the phenomenon was observed and it was possible to establish mathematical diagnoses of cardiac systems regardless of causal, statistical or other considerations.

The law of Zipf-Mandelbrot has allowed studying biomedical phenomena. The degrees of complexity of the specific T repertoire were

differentiated against the P9 allergen in an allergic patient, in the presence and absence of interferon α ; likewise, in cell clones Th.³³ In gynecology, a diagnostic method of fetal cardiac systems was developed based on the dynamic components of the system (CDS), by the law of Zipf-Mandelbrot,³⁴ establishing clear differentiations between fetal cardiac systems, overcoming some limitations of the methods that are more frequently used in clinical practice.³⁵

From this perspective, predictions of cardiac dynamics of neonates have been possible.²³ Also, predictions have been made in infectology,³⁶ immunology,³⁷ in molecular biology,³⁸ public health,³⁹ arterial¹¹ and cellular morphometry.^{40,41} Predictions of mortality in the ICU have been achieved,⁴² and diagnoses of cardiac dynamics of the adult have been made based on proportional entropy.^{26,27}

CONCLUSION

The heart rates obey a hyperbolic mathematical self-organization.

Its evaluation by the Zipf-Mandelbrot law allows to establish differences between normality and acute disease, as confirmed by a blind study with 50 continuous Holter monitoring (20 normal and 30 with acute disease). The results showed that the degree of complexity decreases with the worsening of the cardiac dynamics, achieving objective and reproducible quantifications of cardiac status.

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REFERENCES

- Mandelbrot B. Scaling and power laws without geometry. In: *The fractal geometry of nature*. San Francisco: W. H. Freeman and Co.; 1972. pp. 344-348.
- Zipf GK. *The human behavior and the principle of least effort*. Cambridge, M.A.: Addison-Wesley Press; 1949.
- Mandelbrot B. Information theory and psycholinguistics: a theory of words frequencies. In: Lazafeld P, Henry N (eds.). *Readings in mathematical social science*. Cambridge, MA: MIT Press; 1966.
- Mandelbrot B. Structure formelle des textes et communication. *World*. 1954; 10: 1-27.
- OMS. Centro de prensa. Enfermedades cardiovasculares. Disponible en: <http://www.who.int/mediacentre/factsheets/fs317/es/>
- Carvajal R, Vallverdú M, Caminal P. Análisis no lineal de la variabilidad de la frecuencia cardiaca en casos normales y cardiopatías. *Rev Mex Ing Biomed*. 2000; 21: 29-33.
- Shahbazi F, Asl BM. Generalized discriminant analysis for congestive heart failure risk assessment based on long-term heart rate variability. *Comput Methods Programs Biomed*. 2015; 122 (2): 191-198.
- Lakusic N, Mahovic D, Kruzliak P, Cerkez Habek J, Novak M, Cerovec D. Changes in heart rate variability after coronary artery bypass grafting and clinical importance of these findings. *Biomed Res Int*. 2015; 2015: 680515. doi: 10.1155/2015/680515. Epub 2015 May 20.
- Gallo J, Farbiarz J, Alvarez D. Análisis espectral de la variabilidad de la frecuencia cardiaca. *IATREIA*. 1999; 12 (2): 61-71.
- Goldberger AL, Amaral LA, Hausdorff JM, Ivanov PCh, Peng CK, Stanley HE. Fractal dynamics in physiology: alterations with disease and aging. *Proc Natl Acad Sci U S A*. 2002; 99 Suppl 1: 2466-2472.
- Rodríguez JO, Prieto SE, Correa C, Bernal PA, Puerta GE, Vitery S et al. Theoretical generalization of normal and sick coronary arteries with fractal dimensions and the arterial intrinsic mathematical harmony. *BMC Med Phys*. 2010; 10: 1.
- Rodríguez L, Prieto S, Correa C, Bernal P, Álvarez L, Forero G et al. Diagnóstico fractal del ventriculograma cardiaco izquierdo. *Geometría fractal del ventriculograma durante la dinámica cardiaca*. *Rev Colomb Cardiol*. 2012; 19 (1): 18-24.
- Goldberger AL, Rigney DR, Mietus J, Antman EM, Greenwald S. Nonlinear dynamics in sudden cardiac death syndrome: heart rate oscillations and bifurcations. *Experientia*. 1988; 44 (11-12): 983-987.
- Godoy J, Aníón M, Torres M. Análisis multifractal de la regulación autonómica del ritmo cardíaco en episodios isquémicos. *Rev Argent Bioing*. 2003; 9 (2): 24-29.
- Vanerio-Balbela G, Vidal-Amaral JL, Fernández-Banizi P, López-Achigar G, Banina-Aguerre D, Viana P et al. ¿Se puede predecir el riesgo de muerte súbita luego de sufrir un infarto de miocardio? *Rev Méd Urug*. 2006; 22 (4): 249-265.
- Chang MC, Peng CK, Stanley HE. Emergence of dynamical complexity related to human heart rate variability. *Phys Rev E Stat Nonlin Soft Matter Phys*. 2014; 90 (6): 062806.
- Porta A, Bari V, Marchi A, De Maria B, Cysarz D, Van Leeuwen P et al. Complexity analyses show two distinct types of nonlinear dynamics in short heart period variability recordings. *Front Physiol*. 2015; 6: 71.
- Rodríguez J. Nuevo diagnóstico físico y matemático de la monitoria fetal: predicción de aplicación clínica. *Momento Revista de Física*. 2012; 44: 49-65.
- Rodríguez-Velásquez J, Prieto-Bohórquez S, Ortíz-Salamanca L, Bautista-Charry A, Bernal P, Avilán-Vargas N. Diagnóstico matemático de la monitoria fetal aplicando la ley de Zipf-Mandelbrot. *Rev Fac Med*. 2006; 54 (2): 96-107.
- Rodríguez J. Entropía proporcional de los sistemas dinámicos cardiacos: predicciones físicas y matemáticas de la dinámica cardiaca de aplicación clínica. *Rev Colomb Cardiol*. 2010; 17 (3): 115-129.
- Rodríguez J. Mathematical law of chaotic cardiac dynamic: predictions of clinic application. *J Med Med Sci*. 2011; 2 (8): 1050-1059.
- Rodríguez J, Prieto S, Flórez M, Alarcón C, López R, Aguirre G et al. Physical-mathematical diagnosis of cardiac dynamic on neonatal sepsis: predictions of clinical application. *J Med Med Sci*. 2014; 5 (5): 102-108.
- Rodríguez J, Narváez R, Prieto S, Correa C, Bernal P, Aguirre G et al. The mathematical law of chaotic dynamics applied to cardiac arrhythmias. *J Med Med Sci*. 2013; 4 (7): 291-300.
- Rodríguez J, Álvarez L, Tapia D, López F, Cardona DM, Mora J et al. Evaluación de la dinámica cardiaca de pacientes con arritmia con base en la teoría de la probabilidad. *Medicina*. 2012; 34 (1): 7-16.
- Rodríguez J, Correa C, Melo M, Domínguez D, Prieto S, Cardona DM et al. Chaotic cardiac law: developing predictions of clinical application. *J Med Med Sci*. 2013; 4 (2): 79-84.
- Rodríguez J, Prieto S, Domínguez D, Melo M, Mendoza F, Correa C et al. Mathematical-physical prediction of cardiac dynamics using the proportional entropy of dynamic systems. *J Med Med Sci*. 2013; 4 (8): 370-381.
- Rodríguez J, Prieto S, Bernal P et al. Entropía proporcional aplicada a la evolución de la dinámica cardiaca. Predicciones de aplicación clínica. En: Rodríguez LG (coordinador). *La emergencia de los enfoques de la complejidad en América Latina: desafíos, contribuciones y compromisos para abordar los problemas complejos del siglo XXI*. Tomo 1. Buenos Aires: Comunidad Editora Latinoamericana; 2015. pp. 315-344.
- Rodríguez JO, Prieto SE, Correa SC, Mendoza F, Weiz G, Soracipa MY et al. Physical mathematical evaluation of the cardiac dynamic applying the Zipf – Mandelbrot law. *Journal of Modern Physics*. 2015; 6 (13): 1881-1888.
- Rodríguez J, Correa C, Ortiz L, Prieto S, Bernal P, Ayala J. Evaluación matemática de la dinámica cardiaca con la teoría de la probabilidad. *Rev Mex Cardiol*. 2009; 20 (4): 183-189.
- Rodríguez J, Correa C, Prieto S, Bernal P, Germán F, Salazar G et al. Confirmación del método de ayuda diagnóstica de la dinámica cardiaca de aplicación clínica desarrollado con base en la teoría de la probabilidad. *Rev Fac Med*. 2011; 19 (2): 167-177.

31. Huikuri HV, Mäkikallio TH, Peng CK, Goldberger AL, Hintze U, Møller M. Fractal correlation properties of R-R interval dynamics and mortality in patients with depressed left ventricular function after an acute myocardial infarction. *Circulation*. 2000; 101 (1): 47-53.
32. Voss A, Schulz S, Schroeder R, Baumert M, Caminal P. Methods derived from nonlinear dynamics for analysing heart rate variability. *Philos Trans A Math Phys Eng Sci*. 2009; 367 (1887): 277-296.
33. Rodríguez-Velásquez J. Comportamiento fractal del repertorio T específico contra el alérgeno Poa P9. *Rev Fac Med*. 2005; 53 (2): 72-78.
34. Rodríguez J. Dynamical systems theory and ZIPF – Mandelbrot Law applied to the development of a fetal monitoring diagnostic methodology. XVIII FIGO World Congress of Gynecology and Obstetrics. Kuala Lumpur, MALAYSIA. November 2006.
35. Borgatta L, ShROUT PE, Divon MY. Reliability and reproducibility of nonstress test readings. *Am J Obstet Gynecol*. 1988; 159 (3): 554-558.
36. Rodríguez JO, Prieto SE, Correa C, Pérez CE, Mora JT, Bravo J et al. Predictions of CD4 lymphocytes' count in HIV patients from complete blood count. *BMC Med Phys*. 2013; 13 (1): 3.
37. Rodríguez J, Bernal P, Álvarez L, Pabón S, Ibáñez S, Chapuel N et al. Predicción de unión de péptidos de MSP-1 y EBA-140 de *Plasmodium falciparum* al HLA clase II. Probabilidad, combinatoria y entropía aplicadas a secuencias peptídicas. *Inmunología*. 2010; 29 (3): 91-99.
38. Rodríguez J, Bernal P, Prieto S, Correa C. Teoría de péptidos de alta unión de malaria al glóbulo rojo. Predicciones teóricas de nuevos péptidos de unión y mutaciones teóricas predictivas de aminoácidos críticos. *Inmunología*. 2010; 29(1):7-19.
39. Rodríguez J. Método para la predicción de la dinámica temporal de la malaria en los municipios de Colombia. *Rev Panam Salud Pública*. 2010; 27 (3): 211-218.
40. Prieto-Bohórquez SE, Velásquez JO, Correa-Herrera SC, Soracipa-Muñoz MY. Diagnosis of cervical cells based on fractal and Euclidian geometrical measurements: Intrinsic Geometric Cellular Organization. *BMC Med Phys*. 2014; 14: 2.
41. Velásquez JO, Bohórquez SE, Herrera SC, Cajeli DD, Velásquez DM, de Alonso MM. Geometrical nuclear diagnosis and total paths of cervical cell evolution from normality to cancer. *J Cancer Res Ther*. 2015; 11 (1): 98-104.
42. Rodríguez J. Dynamical systems applied to dynamic variables of patients from the Intensive Care Unit (ICU). Physical and mathematical Mortality predictions on ICU. *J Med Med Sci*. 2015; 6 (8): 102-108.

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